

# The Pennsylvania System of School Assessment

# Mathematics Item and Scoring Sampler



2023-2024 Grade 5

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#### INTRODUCTION

#### **General Introduction**

The Pennsylvania Department of Education (PDE) provides districts and schools with tools to assist in delivering focused instructional programs aligned with the Pennsylvania Core Standards (PCS). These tools include Academic Standards, Assessment Anchors and Eligible Content (AAEC) documents, assessment handbooks, and content-based item and scoring samplers. This Item and Scoring Sampler is a useful tool for Pennsylvania educators in preparing local instructional programs by providing samples of test item types and scored student responses. The item sampler is not designed to be used as a pretest, a curriculum, or any other benchmark for operational testing.

This Item and Scoring Sampler is available in Braille format. For more information regarding Braille, call (717) 901-2238.

#### Pennsylvania Core Standards (PCS)

This sampler contains examples of test questions designed to assess the Pennsylvania Assessment Anchors and Eligible Content aligned to the PCS. The Mathematics, Reading, and Writing PSSA transitioned to PCS-based operational Mathematics and English Language Arts assessments starting with the spring 2015 PSSA administration.

The PCS-aligned Assessment Anchors and Eligible Content documents are posted on this portal:

www.education.pa.gov [Hover over "Data and Reporting," select "Assessment and Accountability," and select "PSSA-PA System of School Assessment." Then select "Assessment Anchors/Eligible Content" on the right side of the screen.]

#### What Is Included

This sampler contains test questions, or test "items," that have been written to align to the Assessment Anchors that are based on the PCS. The sample test questions model the types of items that may appear on an operational PSSA. Each sample test question has been through a rigorous review process to ensure alignment with the Assessment Anchors prior to being piloted in an embedded field test within a PSSA assessment and then used operationally on a PSSA assessment. Answer keys, scoring guidelines, and any related stimulus material are also included. Additionally, sample student responses are provided with each open-ended (OE) item to demonstrate the range of responses that students provided in response to these items.

#### **Purpose and Uses**

The items in this sampler may be used<sup>1</sup> as examples for creating assessment items at the classroom level. Classroom teachers may find it beneficial to have students respond to the open-ended item in this sampler. Educators may then use the sampler as a guide to score the responses either independently or together with colleagues within a school or district. This sampler also includes the *General Description of Scoring Guidelines for Mathematics Open-Ended Items* that students will have access to during a PSSA mathematics administration. The general description of scoring guidelines may be distributed to students for use during local assessments and may also be used by educators when scoring local assessments.

#### **Item Format and Scoring Guidelines**

The multiple-choice (MC) items have four answer choices. Each correct response to an MC item is worth one point.

Each OE item is designed to take approximately ten to fifteen minutes to complete. During the administration of the PSSA, students are given additional time as necessary to complete the test items. Each OE item in mathematics is scored using an item-specific scoring guideline based on a 0–4-point scale. In this sampler, every item-specific scoring guideline is combined with examples of student responses that represent each score point to form a practical, item-specific scoring guide.

#### **Item Alignment**

All PSSA items are aligned to statements and specifications included in the Assessment Anchors and Eligible Content Aligned to the Pennsylvania Core Standards. The mathematics content, process skills, directives, and action statements included in the PSSA mathematics questions align with the Assessment Anchor Content Standards. The Eligible Content statements represent the limits of the content of the mathematics questions.

<sup>&</sup>lt;sup>1</sup> The permission to copy and/or use these materials does not extend to commercial purposes.

# Testing Time and Mode of Testing Delivery for the PSSA

The PSSA is delivered in a traditional paper-and-pencil format as well as in an online format. The estimated time to respond to a test question is the same for both methods of test delivery. The following table shows the estimated response time for each item type.

Mathematics Item Type	МС	OE
Estimated Response Time (minutes)	2	10 to 15

During an official test administration, students are given as much additional time as is necessary to complete the test questions.

# **Mathematics Reporting Categories**

The Assessment Anchors are organized into four classifications as listed below.

•	A = Numbers and Operations	•	C = Geometry
•	B = Algebraic Concepts	•	D = Data Analysis and Probability

These four classifications are used throughout the grade levels. In addition to these classifications, there are five Reporting Categories for each grade level. The first letter of each Reporting Category represents the classification; the second letter represents the Domain as stated in the Common Core State Standards for Mathematics. Listed below are the Reporting Categories for Grade 5.

- A-T = Numbers and Operations in Base Ten
- A-F = Numbers and Operations Fractions
- B-O = Operations and Algebraic Thinking
- C-G = Geometry
- D-M = Measurement and Data

Examples of MC and OE items assessing these categories are included in this sampler.

#### **Item and Scoring Sampler Format**

This sampler includes the test directions and scoring guidelines that appear in the PSSA Mathematics assessments. Each MC item is followed by a table that includes the item alignment, the answer key, the depth of knowledge (DOK) level, the percentage<sup>2</sup> of students who chose each answer option, and a brief answer-option analysis or rationale. The OE item is followed by a table that includes the item alignment, the DOK level, and the mean student score. Additionally, each of the included item-specific scoring guidelines is combined with sample student responses representing each score point to form a practical item-specific scoring guide. The *General Description of Scoring Guidelines for Mathematics Open-Ended Items* used to develop the item-specific scoring guidelines should be used if any additional item-specific scoring guidelines are created for use within local instructional programs. The student responses in this item and scoring sampler are actual student responses; however, the handwriting has been changed to protect the students' identities and to make the item and scoring sampler accessible to as many people as possible.

#### **Example Multiple-Choice Item Information Table**

Item Information	
Alignment	Assigned AAEC
Answer Key	Correct Answer
Depth of Knowledge	Assigned DOK
p-value A	Percentage of students who selected option A
p-value B	Percentage of students who selected option B
p-value C	Percentage of students who selected option C
p-value D	Percentage of students who selected option D
Option Annotations	Brief answer-option analysis or rationale

#### **Example Open-Ended Item Information Table**

Alignment	Assigned AAEC	Depth of Knowledge	Assigned DOK	Mean Score	Average Score
	AALO	Kilowieuge	DON		Score

<sup>&</sup>lt;sup>2</sup> All *p*-value percentages listed in the item information tables have been rounded.

# **General Description of Scoring Guidelines for Mathematics Open-Ended Items**

4—The response demonstrates a *thorough* understanding of the mathematical concepts and procedures required by the task.

The response provides correct answer(s) with clear and complete mathematical procedures shown and a correct explanation, as required by the task. The response may contain a minor "blemish" or omission in work or explanation that does not detract from demonstrating a *thorough* understanding.

3—The response demonstrates a *general* understanding of the mathematical concepts and procedures required by the task.

The response and explanation (as required by the task) are mostly complete and correct. The response may have minor errors or omissions that do not detract from demonstrating a *general* understanding.

2—The response demonstrates a *partial* understanding of the mathematical concepts and procedures required by the task.

The response is somewhat correct with *partial* understanding of the required mathematical concepts and/or procedures demonstrated and/or explained. The response may contain some work that is incomplete or unclear.

- 1—The response demonstrates a *minimal* understanding of the mathematical concepts and procedures required by the task.
- 0—The response has no correct answer and *insufficient* evidence to demonstrate any understanding of the mathematical concepts and procedures required by the task for that grade level.

The response may show only information copied from the question.

Special Categories within zero reported separately:

BLK (blank)	.ls blank, is entirely erased, or gives a written refusal to respond
OT	.ls off-task
LOE	ls in a language other than English
II	Is illegible

#### **Grade 5 Formula Sheet**

Formulas and conversions that you may need on this test are found below. You may refer back to this page at any time during the mathematics test.

2023 Grade 5

#### **Standard Conversions**

- 1 mile (mi) = 1,760 yards (yd)
- 1 mile = 5,280 feet (ft)
- 1 yard (yd) = 3 feet (ft)
- 1 foot = 12 inches (in.)
- 1 ton (T) = 2,000 pounds (lb)
- 1 pound = 16 ounces (oz.)
- 1 gallon (gal) = 4 quarts (gt)
- 1 quart = 2 pints (pt)
- 1 pint = 2 cups (c)
- 1 cup = 8 fluid ounces (fl oz.)

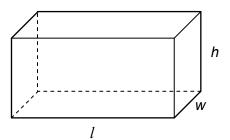
#### **Metric Conversions**

- 1 kilometer (km) = 1,000 meters (m)
- 1 meter = 100 centimeters (cm)
- 1 centimeter = 10 millimeters (mm)
- 1 kilogram (kg) = 1,000 grams (g)
- 1 liter (L) = 1,000 milliliters (mL)

#### **Time Conversions**

- 1 century = 10 decades
- 1 decade = 10 years (yr)
- 1 year (yr) = 12 months (mo)
- 1 year = 52 weeks (wk)
- 1 year = 365 days
- 1 week = 7 days
- 1 day = 24 hours (hr)
- 1 hour = 60 minutes (min)
- 1 minute = 60 seconds (sec)

#### **Rectangular Prism**



Volume = length × width × height  $V = l \times w \times h$ 

Volume = area of the base  $\times$  height  $V = B \times h$ 

Volume = area of the base  $\times$  width  $V = B \times w$ 

Volume = area of the base  $\times$  length  $V = B \times l$ 

#### MATHEMATICS TEST DIRECTIONS

On the following pages are the mathematics questions.

 You may <u>not</u> use a calculator for question 1. You may use a calculator for all other questions on this test.

#### **Directions for Multiple-Choice Questions**

Some questions will ask you to select an answer from among four choices.

For the multiple-choice questions:

- First solve the problem on scratch paper.
- Choose the correct answer and record your choice in the answer booklet.
- If none of the choices matches your answer, go back and check your work for possible errors.
- Only one of the answers provided is the correct response.

#### **Directions for Open-Ended Questions**

Some questions will require you to write your response.

For the open-ended questions:

- These questions have more than one part. Be sure to read the directions carefully.
- You cannot receive the highest score for an open-ended question without completing all tasks in the question. For example, if the question asks you to show your work or explain your reasoning, be sure to show your work or explain your reasoning in the space provided.
- If the question does **not** ask you to show your work or explain your reasoning, you
  may use the space provided, but only those parts of your response that the question
  specifically asks for will be scored.
- Write your response in the appropriate location within the response box in the
  answer booklet. Some answers may require graphing, plotting, labeling, drawing, or
  shading. If you use scratch paper, be sure to transfer your final response and any
  needed work or reasoning to the answer booklet.

Question 1 in this sampler is to be solved without the use of a calculator.

# **MULTIPLE-CHOICE ITEMS**

**1.** Subtract: 1.76 – 0.9

A. 0.86

B. 1.26

C. 1.67

D. 1.73

Item Information	
Alignment	A-T.2.1.3
Answer Key	A
Depth of Knowledge	1
p-value A	59% (correct answer)
p-value B	8%
p-value C	27%
p-value D	6%
Option Annotations	<ul> <li>A. Correct: aligns the decimals before subtracting OR includes a 0 in the hundredths place of 0.9 and then subtracts 1.76 – 0.90</li> <li>B. subtracts the 7 from the 9</li> <li>C. subtracts 0.09 from 1.76 (right-aligns the numbers before subtracting)</li> <li>D. subtracts 0.09 from 1.76 (right-aligns the numbers before subtracting) and subtracts the 6 from the 9</li> </ul>

#### A calculator is permitted for use in solving questions 2–17 in this sampler.

2. The expression below represents the mass, in grams, of a mineral sample.

$$7 \times 10 + 3 \times 0.1 + 9 \times 0.001$$

What is the mass, in grams, of the mineral sample?

- A. seventy and thirty-nine hundredths
- B. seventy-three and nine hundredths
- C. seventy-three and nine thousandths
- D. seventy and three hundred nine thousandths

Item Information	
Alignment	A-T.1.1.3
Answer Key	D
Depth of Knowledge	1
p-value A	15%
p-value B	9%
p-value C	17%
p-value D	59% (correct answer)
Option Annotations	<ul> <li>A. treats the last digit as hundredths</li> <li>B. uses 3 in the ones place rather than the tenths place and treats the last digit as hundredths</li> <li>C. uses 3 in the ones place rather than the tenths place</li> <li>D. Correct: recognizes that 7 × 10 = 70, 3 × 0.1 = 0.3, and 9 × 0.001 = 0.009; adds these values together and determines the sum is 70.309; and then uses "seventy" to represent 70 (the digits to the left of the decimal point), "and" to represent the decimal point (separates the whole part of the number from the decimal part of the number), "three hundred nine" to represent 309 (the digits to the right of the decimal point), and "thousandths" since the rightmost digit is in the thousandths place</li> </ul>

- **3.** Which statement correctly compares  $2 \times 100 + 4 \times 1 + 5 \times 0.1$  and 204.05?
  - A. 204.5 < 204.05
  - B. 204.5 > 204.05
  - C. 204.05 = 204.05
  - D. 204.005 < 204.05

Item Information	
Alignment	A-T.1.1.4
	A-T.1.1.3
Answer Key	В
Depth of Knowledge	1
p-value A	16%
p-value B	48% (correct answer)
p-value C	32%
p-value D	4%
Option Annotations	<ul> <li>A. reverses the inequality symbol</li> <li>B. Correct: recognizes 2 × 100 = 200, 4 × 1 = 4, 5 × 0.1 = 0.5; adds these values together and determines the sum is 204.5; compares the whole-number parts (204 = 204), and then either compares 5 tenths to 0 tenths, recognizing that .5 &gt; .0 OR writes 0.5 as 0.50 to compare the decimal parts (0.50 &gt; 0.05)</li> <li>C. uses 5 × 0.1 = 0.05 rather than 0.5</li> <li>D. uses 5 × 0.1 = 0.005 rather than 0.5</li> </ul>

- **4.** A bakery owner orders 6 cases of chocolate. Each case contains 4 blocks of chocolate. Each block weighs 13.2 pounds. How many pounds of chocolate does the bakery owner order?
  - A. 58.8
  - B. 83.2
  - C. 103.2
  - D. 316.8

Item Information	
Alignment	A-T.2.1
Answer Key	D
Depth of Knowledge	2
p-value A	13%
p-value B	11%
p-value C	8%
p-value D	68% (correct answer)
Option Annotations	<ul> <li>A. multiplies 4 by 13.2 and then adds 6 to the product [4 × 13.2 + 6]</li> <li>B. multiplies 6 by 13.2 and then adds 4 to the product [6 × 13.2 + 4]</li> <li>C. adds 4 to 13.2 and then multiplies the sum by 6 [(4 + 13.2) × 6]</li> <li>D. Correct: multiplies 6 by 4 to determine that the product is 24 blocks of chocolate and then multiplies 24 by 13.2 to determine that the product is 316.8 pounds of chocolate</li> </ul>

- 5. A farmer has 10 packages of corn seeds. Each package contains 300 seeds. He plants all the seeds in 20 rows with an equal number of seeds in each row. How many seeds are in each row?
  - A. 150
  - B. 600
  - C. 1,500
  - D. 60,000

Item Information	
Alignment	A-T.2.1.2
	A-T.2.1.1
Answer Key	A
Depth of Knowledge	1
p-value A	62% (correct answer)
p-value B	10%
p-value C	8%
p-value D	20%
Option Annotations	<ul> <li>A. Correct: multiplies 10 by 300 to determine that the product is 3,000 seeds and then divides 3,000 by 20 to determine that the quotient is 150 seeds in each row</li> <li>B. calculates 300 ÷ 10 × 20</li> <li>C. calculates 30 ÷ 2 × 100</li> <li>D. calculates 300 × 10 × 20</li> </ul>

- **6.** Which expression is equivalent to  $\frac{1}{3} + \frac{1}{30} \frac{1}{5}$ ?
  - A.  $\frac{1}{3} + \frac{6}{30} \frac{1}{30}$
  - B.  $\frac{5}{15} \frac{3}{15} + \frac{1}{30}$
  - C.  $\frac{1}{30} + \frac{1}{30} \frac{1}{5}$
  - D.  $\frac{5}{15} + \frac{3}{15} \frac{1}{30}$

Item Information	A-F.1.1.1
Alignment Answer Kov	В
Answer Key	
Depth of Knowledge	2
p-value A	12%
p-value B	51% (correct answer)
p-value C	23%
p-value D	14%
Option Annotations	A. converts $\frac{1}{5}$ to $\frac{6}{30}$ correctly but does not keep the minus sign with
	the $\frac{6}{30}$ when using the commutative property to change the order of
	the terms
	B. Correct: converts $\frac{1}{3}$ to $\frac{5}{15}$ by multiplying both the numerator
	and the denominator by 5, converts $\frac{1}{5}$ to $\frac{3}{15}$ by multiplying both
	the numerator and the denominator by 3, and then uses the
	commutative property to change the order of the terms " $-\frac{3}{15}$ " and
	"+ $\frac{1}{30}$ "
	C. converts $\frac{1}{3}$ to $\frac{1}{30}$ by multiplying only the denominator by 10
	D. converts $\frac{1}{3}$ to $\frac{5}{15}$ and $\frac{1}{5}$ to $\frac{3}{15}$ correctly but does not keep the minus
	sign with the $\frac{3}{15}$ when using the commutative property to change
	the order of the terms

- 7. Mrs. Brown has a package containing n pounds of cereal. Every day she puts  $\frac{1}{8}$  pound of cereal into her son's lunchbox and  $\frac{1}{8}$  pound of cereal into her daughter's lunchbox. Which expression represents the number of days Mrs. Brown can do this before she runs out of cereal?
  - A.  $(n \times 2) \times \frac{1}{8}$
  - B.  $(n \times 2) \div \frac{1}{8}$
  - C.  $n \times \left(2 \times \frac{1}{8}\right)$
  - D.  $n \div \left(2 \times \frac{1}{8}\right)$

Item Information			
Alignment	A-F.2.1		
Answer Key	D		
Depth of Knowledge	2		
p-value A	17%		
p-value B	20%		
p-value C	26%		
p-value D	37% (correct answer)		
Option Annotations	<ul> <li>A. doubles the amount because there are two children and multiplies by the daily amount rather than dividing by the daily amount</li> <li>B. doubles the amount because there are two children</li> <li>C. multiplies by the daily amount rather than dividing by the daily amount</li> </ul>		
	D. Correct: recognizes that $\frac{1}{8}$ should be multiplied by 2 before dividing the total amount by that product		

- **8.** Keira has 8 cups of juice. She pours the juice into 5 glasses, pouring the same amount of juice into each glass. How many cups of juice are in each glass?
  - A.  $\frac{5}{8}$
  - B.  $1\frac{3}{8}$
  - C.  $1\frac{3}{5}$
  - D. 3

Item Information			
Alignment	A-F.2.1.1		
Answer Key	C		
Depth of Knowledge	1		
p-value A	29%		
p-value B	18%		
p-value C	43% (correct answer)		
p-value D	10%		
Option Annotations	<ul> <li>A. divides 5 by 8</li> <li>B. writes the incorrect denominator when converting the improper fraction into a mixed number</li> <li>C. Correct: determines that 8 cups divided among 5 glasses results in 1 with a remainder of 3 and then writes the remainder as the fraction 3 over 5</li> <li>D. subtracts 5 from 8</li> </ul>		

- 9. Alli and Bert each have some money. Bert has  $\frac{5}{4}$  as many dollars as Alli has. Which statement about the amount of money Alli and Bert each have is true?
  - A. Alli has more money than Bert has.
  - B. Bert has more money than Alli has.
  - C. Alli and Bert have the same amount of money.
  - D. There is not enough information to compare the amount of money Alli and Bert each have.

Item Information			
Alignment	A-F.2.1.3		
Answer Key	В		
Depth of Knowledge	2		
p-value A	15%		
<i>p</i> -value B	48% (correct answer)		
<i>p</i> -value C	14%		
p-value D	23%		
Option Annotations	<ul> <li>A. does not recognize that <sup>5</sup>/<sub>4</sub> is greater than 1 and multiplying any number by a fraction greater than 1 will result in a product larger than either factor</li> <li>B. Correct: recognizes that <sup>5</sup>/<sub>4</sub> is greater than 1 and that multiplying any number by a fraction greater than 1 will result in a product larger than either factor</li> </ul>		
	C. does not recognize that $\frac{5}{4}$ is greater than 1  D. thinks it is not possible to make a comparison about the amount of		
	money either person has since no exact values are given		

- **10.** A relay race is  $\frac{1}{8}$  mile long. Each relay team has 4 members. Each team member runs the same distance. How many miles does each team member run?
  - A.  $\frac{1}{2}$
  - B.  $\frac{1}{4}$
  - C.  $\frac{1}{12}$
  - D.  $\frac{1}{32}$

Item Information			
Alignment	A-F.2.1.4		
Answer Key	D		
Depth of Knowledge	2		
p-value A	27%		
p-value B	15%		
p-value C	10%		
p-value D	48% (correct answer)		
Option Annotations	A. multiplies 4 and $\frac{1}{8}$		
	<ul><li>B. determines the fraction of the race completed by each member [i.e., finds the reciprocal of the number of team members]</li><li>C. adds 8 and 4</li></ul>		
	D. Correct: recognizes that this situation represents dividing $\frac{1}{8}$ by 4,		
	which is the same as multiplying $\frac{1}{8}$ by $\frac{1}{4}$ , resulting in $\frac{1 \times 1}{8 \times 4} = \frac{1}{32}$		

11. Bruce saves \$1 each week. His brother Len saves \$2 each week. They combine their savings each week. Which coordinate grid represents the total amount of money, in dollars, Bruce and Len save over time?

В.

D.

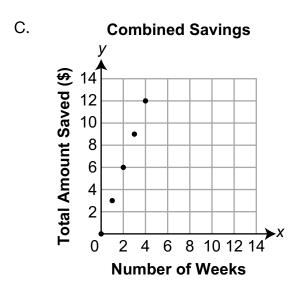
A. **Combined Savings** Total Amount Saved (\$) 12 10 8 6 2

8 10 12 14

**Number of Weeks** 

0

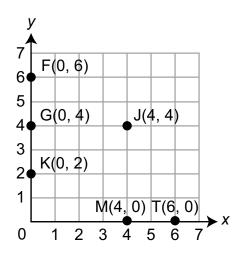
2 4 6





Item Information			
Alignment	C-G.1		
Answer Key	С		
Depth of Knowledge	2		
p-value A	20%		
p-value B	18%		
p-value C	48% (correct answer)		
p-value D	14%		
Option Annotations	<ul> <li>A. uses Bruce's savings as the <i>x</i>-coordinates and Len's savings as the <i>y</i>-coordinates</li> <li>B. uses Bruce's savings as the <i>y</i>-coordinates and Len's savings as the <i>x</i>-coordinates</li> <li>C. Correct: increases each <i>x</i>-coordinate by 1 since this represents the number of weeks and increases each <i>y</i>-coordinate by 3 since this represents the two brothers saving a total of \$3 each week</li> <li>D. uses the weekly total savings as the <i>x</i>-coordinates and the numbers of weeks as the <i>y</i>-coordinates</li> </ul>		

12. A coordinate grid is shown below.



Which two points on the coordinate grid have the same *y*-coordinate?

- A. point G and point K
- B. point J and point M
- C. point G and point J
- D. point F and point T

Item Information			
Alignment	C-G.1.1.1		
Answer Key	С		
Depth of Knowledge	1		
p-value A	17%		
p-value B	13%		
p-value C	53% (correct answer)		
p-value D	17%		
Option Annotations	<ul> <li>A. selects two points on the <i>y</i>-axis</li> <li>B. selects two points with the same <i>x</i>-coordinate</li> <li>C. Correct: either selects two points that have the same second coordinate since the second coordinate of an ordered pair represents the <i>y</i>-coordinate OR selects two points on the same horizontal line since the <i>y</i>-coordinate represents the distance from the <i>x</i>-axis</li> <li>D. selects two points that have the <i>x</i>-coordinate and <i>y</i>-coordinate switched</li> </ul>		

**13.** The graph below represents the amount of coffee brewed (y), in ounces, based on the amount of time (x), in minutes, for which the coffee maker has been brewing coffee.



- Which ordered pair represents the number of ounces of coffee brewed when the coffee maker has been brewing coffee for 5 minutes?
- A. (5, 10)
- B. (5, 11)
- C. (10, 5)
- D. (11, 5)

Item Information			
Alignment	C-G.1.1.2		
Answer Key	A		
Depth of Knowledge	1		
p-value A	63% (correct answer)		
p-value B	19%		
p-value C	12%		
p-value D	6%		
Option Annotations	<ul> <li>A. Correct: recognizes that the <i>x</i>-coordinate represents the amount of time, so uses 5 as the first coordinate of the ordered pair; looks at the line directly above the 5 on the <i>x</i>-axis, sees that it is halfway between the 8 and 12 grid lines, and uses 10 as the second coordinate of the ordered pair since 10 is halfway between 8 and 12</li> <li>B. selects a <i>y</i>-value that is 1 less than 12 (using a <i>y</i>-scale of 2 rather than 4)</li> <li>C. reverses the ordered pair</li> <li>D. selects a <i>y</i>-value that is 1 less than 12 (using a <i>y</i>-scale of 2 rather than 4) and reverses the ordered pair</li> </ul>		

- 14. Which term does not describe a square?
  - A. parallelogram
  - B. rectangle
  - C. rhombus
  - D. trapezoid

Item Information			
Alignment	C-G.2.1.1		
Answer Key	D		
Depth of Knowledge	1		
p-value A	10%		
p-value B	10%		
p-value C	15%		
p-value D	65% (correct answer)		
Option Annotations	<ul> <li>A. does not account for a parallelogram with 4 right angles and 4 equal sides OR does not recognize that a square is a parallelogram because a square has 2 pairs of parallel sides</li> <li>B. does not account for a rectangle with 4 equal sides OR does not recognize that a square is a rectangle because all 4 angles are right angles</li> </ul>		
	<ul> <li>C. does not account for a rhombus with 4 right angles OR does not recognize that a square is a rhombus because all 4 sides are equal</li> <li>D. Correct: recognizes that a trapezoid has only 1 pair of parallel sides and that a square has 2 pairs of parallel sides</li> </ul>		

- **15.** Tracy needs a **gallon** of water, but she has only **quart**-sized, **pint**-sized, and **cup**-sized containers.
  - She first fills one **quart**-sized container with water.
  - She then fills some **pint**-sized containers and some **cup**-sized containers with water.

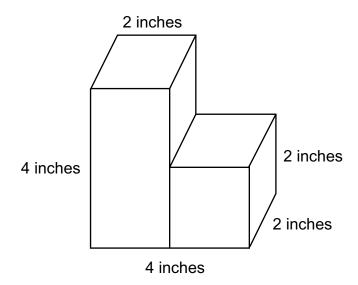
How many **pint**-sized containers and **cup**-sized containers could Tracy fill to have a total of 1 **gallon** of water in all the containers?

- A. 1 pint-sized container and 2 cup-sized containers
- B. 2 pint-sized containers and 1 cup-sized container
- C. 2 pint-sized containers and 5 cup-sized containers
- D. 5 pint-sized containers and 2 cup-sized containers

Item Information				
Alignment	D-M.1.1.1			
Answer Key	D			
Depth of Knowledge	2			
p-value A	15%			
p-value B	16%			
p-value C	31%			
p-value D	38% (correct answer)			
Option Annotations	<ul> <li>A. thinks there are only 2 quarts in a gallon</li> <li>B. thinks there are only 2 quarts in a gallon and confuses cups and pints</li> <li>C. confuses cups and pints</li> <li>D. Correct: either calculates 5 pints + 2 cups = 5 pints + 1 pint = 6 pints = 3 quarts and 3 quarts + 1 quart = 4 quarts = 1 gallon OR calculates 1 gallon - 1 quart = 4 quarts - 1 quart = 3 quarts = 6 pints = 5 pints + 1 pint = 5 pints + 2 cups</li> </ul>			

**16.** A toy company makes solid game pieces out of plastic. Each game piece is made by connecting two right rectangular prisms as shown in the picture below.

**Game Piece** 



What is the volume, in cubic inches, of plastic needed to make each game piece?

- A. 14
- B. 24
- C. 32
- D. 48

Item Information			
Alignment	D-M.3.1.2		
Answer Key	В		
Depth of Knowledge	2		
p-value A	31%		
p-value B	40% (correct answer)		
p-value C	18%		
p-value D	11%		
Option Annotations	<ul> <li>A. adds the given lengths</li> <li>B. Correct: either recognizes that the prisms have the same width (2 inches), subtracts the length of the taller prism from the overall length to find the length of the shorter prism (4 - 2 = 2), finds the volume of each prism (2 × 2 × 4 = 16 and 2 × 2 × 2 = 8), and then adds the volumes to find the total (16 + 8 = 24) OR multiplies the overall length (4), width (2), and height (4) and then subtracts the volume of the "missing" part above the shorter prism (2 × 2 × 2 = 8), which is 32 - 8 = 24</li> <li>C. multiplies the overall length (4), width (2), and height (4) but does not account for the "missing" part above the shorter prism</li> <li>D. multiplies 4 × 4 × 2 to find the volume of the taller prism, multiplies 4 × 2 × 2 to find the volume of the shorter prism, and then adds the volumes to find the total (32 + 16)</li> </ul>		

#### **OPEN-ENDED QUESTION**

- **17.** Every week, Patrick attends basketball practice for 2 hours on Tuesday and 3 hours on Thursday. Patrick has been attending practice for 6 weeks.
  - **A.** Write a numerical expression with at least one operation symbol to represent the total amount of time Patrick has spent at basketball practice the past 6 weeks.

The expression below represents the number of points Patrick scored in his last basketball game.

$$2 \times (4 + 3) + 3 \times (1 + 2) + 2$$

**B.** How many points did Patrick score in his last game? Show or explain all your work.

Go to the next page to finish question 17.

GO ON

**17.** *Continued.* Please refer to the previous page for task explanation.

During another game, Patrick scored points by making 2-point shots and by making 3-point shots. The two expressions below represent the number of points he scored from making 2-point shots and the number of points he scored from making 3-point shots.

2-point shots: 
$$2 \times (4 + 6)$$

3-point shots: 
$$3 \times (2 + 3)$$

Patrick claims he scored twice as many points from making 2-point shots as from making 3-point shots since 4 + 6 is twice as large as 2 + 3.

**C.** Explain why Patrick's claim is **not** correct even though 4 + 6 is twice as large as 2 + 3.

After you have finished your work, close this booklet so your teacher will know you are finished.



# **Item-Specific Scoring Guideline**

# **#17 Item Information**

Alignment	B-O.1.1.1 B-O.1.1.2	Depth of Knowledge	2	Mean Score	1.43
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# Assessment Anchor this item will be reported under:

M05.B-O.1—Write and interpret numerical expressions.

# **Specific Anchor Descriptor addressed by this item:**

M05.B-O.1.1 — Analyze and complete calculations by applying the order of operations.

# **Scoring Guide**

Score	In this item, the student
4	Demonstrates a thorough understanding of how to write and interpret numerical expressions by correctly solving problems and clearly explaining procedures.
3	Demonstrates a general understanding of how to write and interpret numerical expressions by correctly solving problems and clearly explaining procedures with only minor errors or omissions.
2	Demonstrates a partial understanding of how to write and interpret numerical expressions by correctly performing a significant portion of the required task.
1	Demonstrates minimal understanding of how to write and interpret numerical expressions.
0	The response has no correct answer and insufficient evidence to demonstrate any understanding of the mathematical concepts and procedures as required by the task. Response may show only information copied from the question.

# **Top-Scoring Student Response and Training Notes**

Score	Description
4	Student earns 4 points.
3	Student earns 3.0–3.5 points.
2	Student earns 2.0–2.5 points.
1	OR Student demonstrates minimal understanding of how to write and interpret numerical expressions.
0	Response is incorrect or contains some correct work that is irrelevant to the skill or concept being measured.

# **Top-Scoring Response**

#### Part A (1 point):

1 point for correct answer

OR  $\frac{1}{2}$  point for correct expression as "one side" of equation (e.g.,  $6 \times 5 = 30$ )

Note: No credit for "30" only

What?	Why?
$6 \times (2 + 3)$ <b>OR</b> $6 \times 2 + 6 \times 3$ <b>OR</b> $6 \times 5$	
OR equivalent	

#### Part B (2 points):

1 point for correct answer

1 point for correct and complete support

 $OR \frac{1}{2}$  point for correct but incomplete support

What?	Why?
25 (points)	Sample Work: $2 \times (4 + 3) + 3 \times (1 + 2) + 2$ $2 \times 7 + 3 \times 3 + 2$ 14 + 9 + 2 = 25 OR
	Sample Explanation: First, I simplified the values inside the parentheses $(4 + 3 = 7 \text{ and } 1 + 2 = 3)$ . Next, I multiplied the two pairs of numbers $(2 \times 7 = 14 \text{ and } 3 \times 3 = 9)$ . Then, I added the remaining numbers together $(14 + 9 + 2 = 25)$ . OR equivalent

# Part C (1 point):

1 point for correct and complete explanation

 $OR\frac{1}{2}$  point for correct but incomplete explanation

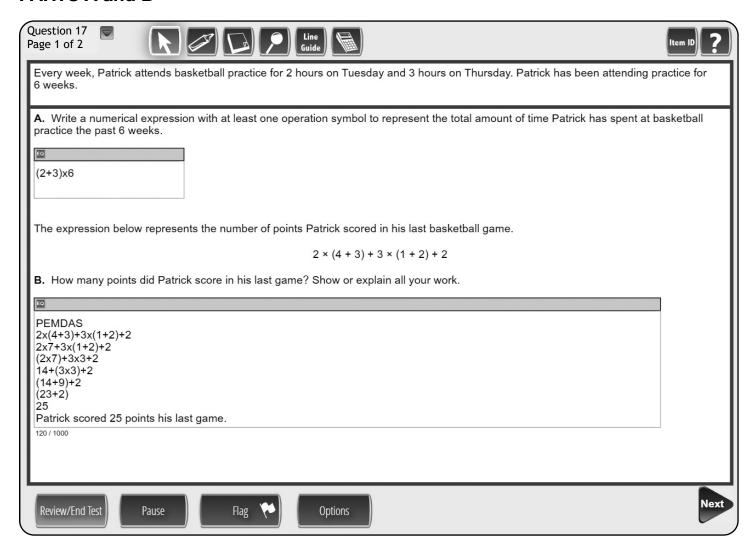
What?	Why?
	Sample Explanation: Two-point shots equal 20 because (4 + 6) is multiplied by 2. Three-point shots equal 15 because (2 + 3) is multiplied by 3. 20 is not twice as large as 15.
	OR equivalent

#### STUDENT RESPONSE

# **Response Score: 4 points**



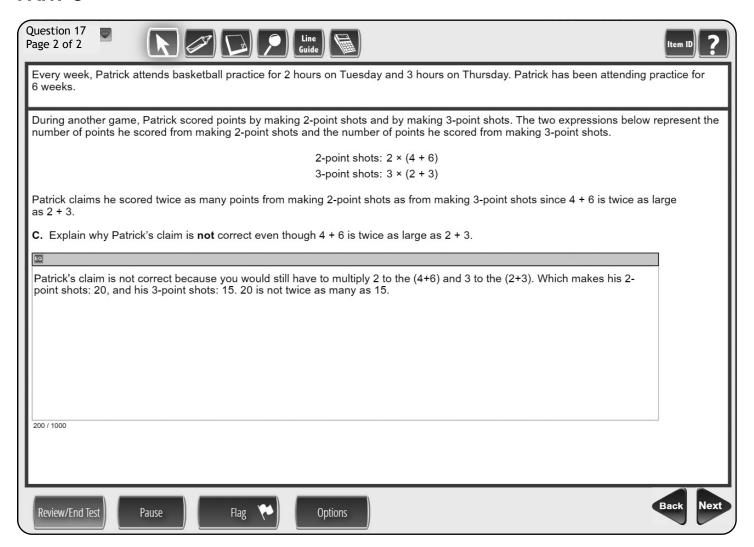
#### **PARTS A and B**



Part A. The student provided a correct expression  $[(2+3)\times6]$ , with the sum (2+3) representing the total amount of time spent at basketball practice each week, which is then multiplied by the number of weeks (6). [1 point]

Part B. The student provided the correct answer (*Patrick scored 25 points his last game.*) with correct and complete support. The work provided shows that the student used PEMDAS to determine the order of operations in solving: first parentheses  $[2\times(4+3)+3\times(1+2)+2\dots(2\times7)+3\times3+2]$ , then multiplication  $[(2\times7)+3\times3+2\dots(14+9)+2]$ , and finally addition  $[(14+9)+2\dots25]$ . [2 points]

#### **PART C**



Part C. The student provided a correct and complete explanation as to why Patrick's claim is not correct. It references the multipliers [you would still have to multiply 2 to the (4+6) and 3 to the (2+3)], evaluates the expressions to get 20 and 15 (Which makes his 2-point shots: 20, and his 3-point shots: 15), and then makes a correct comparison between the two point totals (20 is not twice as many as 15). [1 point]

#### STUDENT RESPONSE

### **Response Score: 3 points**

- **17.** Every week, Patrick attends basketball practice for 2 hours on Tuesday and 3 hours on Thursday. Patrick has been attending practice for 6 weeks.
  - **A.** Write a numerical expression with at least one operation symbol to represent the total amount of time Patrick has spent at basketball practice the past 6 weeks.

Part A. The student provided an incorrect answer in the form of an equation  $[6(2 \times 3) = 30 \text{ hours}]$  rather than an expression. The left side of the equation provided is incorrect: the student used a multiplication sign inside of the parentheses rather than an addition sign. The right side of the equation (30 hours) shows the correct total amount of time but does not match the expression on the left side, which has a value of 36. [0 points]

The expression below represents the number of points Patrick scored in his last basketball game.

$$2 \times (4 + 3) + 3 \times (1 + 2) + 2 = 25$$

B. How many points did Patrick score in his last game? Show or explain all your work. Patrick scored 25 points at his jast game.

What I did was when I saw the parenthezer I knew they came first. 4+3=7 and 1+2=3. So then I made my own equation to make it easier for me to understand.

The Equation was  $2 \times 7 + 3 \times 3 + 2$ . Then I did  $2 \times 7$  and  $3 \times 3$  because in order of operation and multiplication and division 90 first but in this case it's sorly multiplication. So  $2 \times 7 = 14$  and  $3 \times 3 = 9$ . So now your add The numbers you add are 14 + 9 = 23. Then finally you add 2 which gets you to 25 so patrick scored a total of 25 points at his last game.

Equation  $2 \times 7 + 3 \times 3 + 2 = 14 + 9 = 23 + 2 = 25$  points

Part B. The student provided a correct answer (25 points) with correct and complete support. The student explained how the order of operations was used to calculate the given expression's total (I saw the parethenzes I knew they came first. I + I = I and I + I = I so then I made my own equation to make it easier for me . . . I × I + I × I × I + I = I and I × I = I and I × I = I + I = I and I × I = I = I + I = I = I + I = I = I + I = I = I + I = I = I + I = I = I = I + I = I = I = I + I = I

17. Continued. Please refer to the previous page for task explanation.

During another game, Patrick scored points by making 2-point shots and by making 3-point shots. The two expressions below represent the number of points he scored from making 2-point shots and the number of points he scored from making 3-point shots.

3-point shots: 
$$3 \times (2 + 3) = 15$$

Patrick claims he scored twice as many points from making 2-point shots as from making 3-point shots since 4 + 6 is twice as large as 2 + 3.

C. Explain why Patrick's claim is not correct even though 4+6 is twice as large as 2+3. Patrick is not correct because even though 4+6 is greater than 2+3, your not looking at the actual answer. With the 2 points hots he got more points than 3 point shots but it isn't twice as many. 2 point shots equal 20 points and 3 point shots equal 15 points. When you subtract 20-15 it equals 5. That is not twice as many. Twice as many would be if you did 20-10 because 10+10=20. So Patrick isn't correct be cause the total points in general don't add up to be twice as many

Part C. The student provided a correct and complete explanation as to why Patrick's claim is not correct. It references the multipliers (2 point shots and 3 point shots), evaluates the expressions to get 20 and 15 (2 point shots equal 20 points and 3 point shots equal 15 points), and then makes a correct comparison between the two point totals (With the 2 point shots he got more points than 3 point shots but it isn't twice as many. . . . When you subtract 20 – 15 it equals 5. That is not twice as many). [1 point]

After you have finished your work, close this booklet so your teacher will know you are finished.



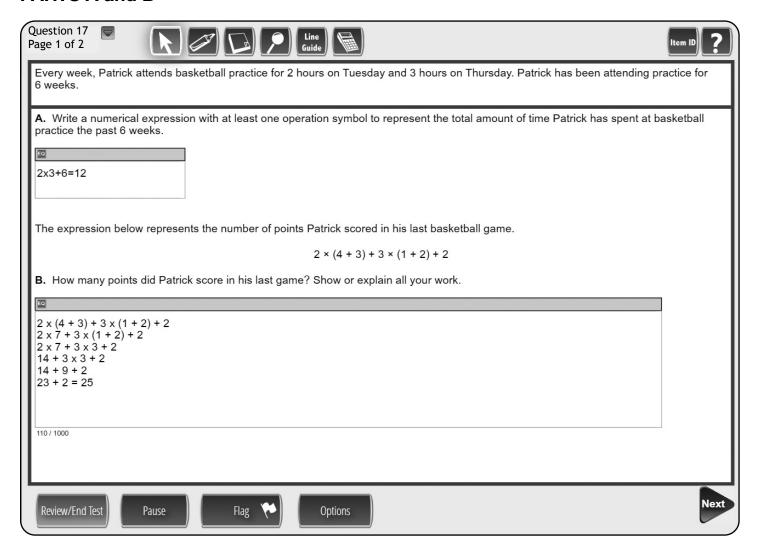
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#### STUDENT RESPONSE

## **Response Score: 2 points**



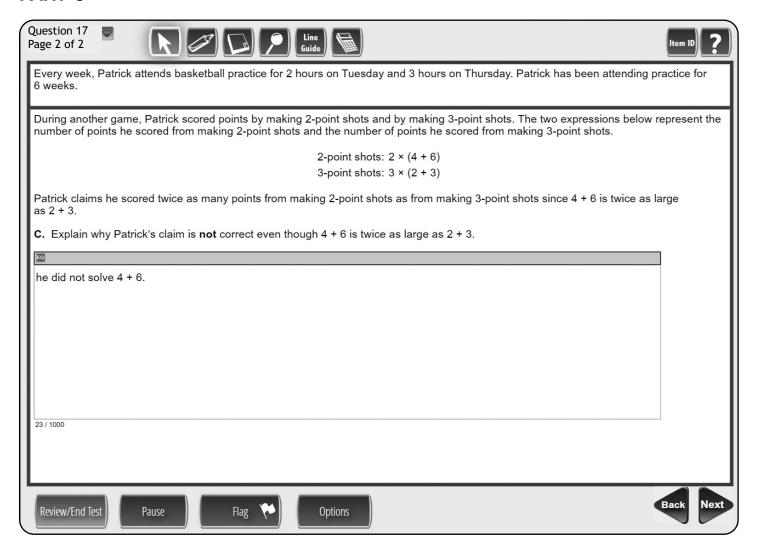
#### **PARTS A and B**



Part A. The student provided an incorrect answer in the form of an equation  $(2\times3+6=12)$  rather than an expression. The left side of the equation provided is incorrect: the student switched the multiplication sign and the addition sign and did not include grouping symbols around the 2 and 3. [0 points]

Part B. The student provided a correct answer (25) with correct and complete support. The work provided shows the student used the order of operations correctly to calculate the given expression's total: first parentheses  $[2 \times (4+3) + 3 \times (1+2) + 2 \rightarrow 2 \times 7 + 3 \times (1+2) + 2]$ , then multiplication  $(2 \times 7 + 3 \times 3 + 2 \rightarrow 14 + 3 \times 3 + 2)$ , and finally addition  $(14+9+2 \rightarrow 23+2=25)$ . [2 points]

#### **PART C**



Part C. The student provided an incorrect explanation (he did not solve 4 + 6) that did not include referencing the multipliers, evaluating the expressions to get 20 and 15, or making a comparison between the two point totals. [0 points]

#### STUDENT RESPONSE

## **Response Score: 1 point**

- **17.** Every week, Patrick attends basketball practice for 2 hours on Tuesday and 3 hours on Thursday. Patrick has been attending practice for 6 weeks.
  - **A.** Write a numerical expression with at least one operation symbol to represent the total amount of time Patrick has spent at basketball practice the past 6 weeks.

Part A. The student provided an incorrect answer  $(2 \times 3 = \underline{\hspace{1cm}} \times 6 = \underline{\hspace{1cm}})$ . [0 points]

The expression below represents the number of points Patrick scored in his last basketball game.

$$2 \times (4 + 3) + 3 \times (1 + 2) + 2$$

**B.** How many points did Patrick score in his last game? Show or explain all your work.

$$2 \times (4+3) + 3 \times (1+2) + 2$$

$$2 \times 7 + 3 \times (1+2) + 2$$

$$2 \times 7 + 3 \times 3 + 2$$

$$14 + 3 \times 3 + 2$$

$$17 \times 3 + 2$$

$$51 + 2 = 53$$

53 points

Part B. The student provided an incorrect answer (53 points) with correct but incomplete support. The work shown included some calculations completed correctly using the order of operations, with parentheses first  $[2 \times (4+3) + 3 \times (1+2) + 2 \dots 2 \times 7 + 3 \times 3 + 2]$  and the first multiplication step  $(2 \times 7 + 3 \times 3 + 2 \rightarrow 14 + 3 \times 3 + 2)$ . The student's next step then incorrectly added 14 and 3 rather than multiplying the  $3 \times 3$ . [0.5 points]

Go to the next page to finish question 17.

GO ON

17. Continued. Please refer to the previous page for task explanation.

During another game, Patrick scored points by making 2-point shots and by making 3-point shots. The two expressions below represent the number of points he scored from making 2-point shots and the number of points he scored from making 3-point shots.

2-point shots:  $2 \times (4 + 6)$  20

3-point shots:  $3 \times (2 + 3)$  \ \forall 5

Patrick claims he scored twice as many points from making 2-point shots as from making 3-point shots since 4 + 6 is twice as large as 2 + 3.

**C.** Explain why Patrick's claim is **not** correct even though 4 + 6 is twice as large as 2 + 3.

because 15 is only 5 away from 20 and 15 is not twice as small as the number 20.

Part C. The student provided a correct but incomplete explanation as to why Patrick's claim is not correct. The student evaluated the expressions to get 20 and 15 in the given information section (2-point shots: 2 × (4 + 6) [=] 20 and 3-point shots: 3 × (2 + 3) [=] 15) and then made a correct comparison between the two point totals (because 15 is only 5 away from 20 and 15 is not twice as small as the number 20); however, the student did not reference the multipliers 2 and 3. [0.5 points]

After you have finished your work, close this booklet so your teacher will know you are finished.

STOP

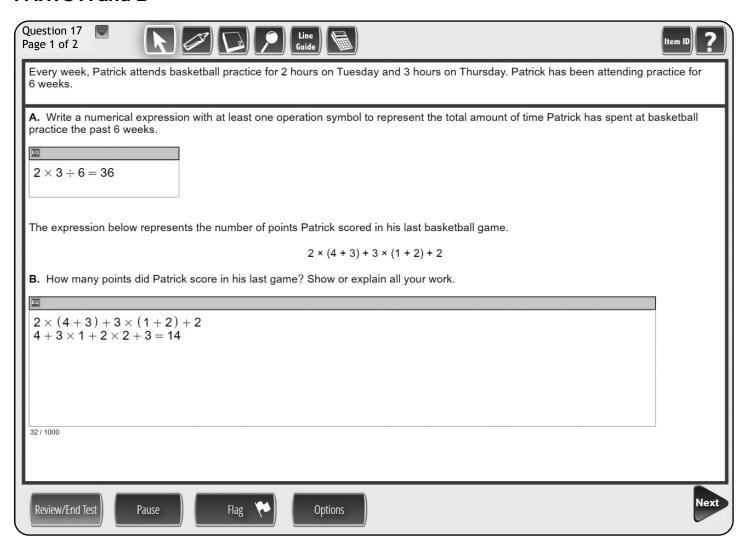
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#### STUDENT RESPONSE

## **Response Score: 0 points**



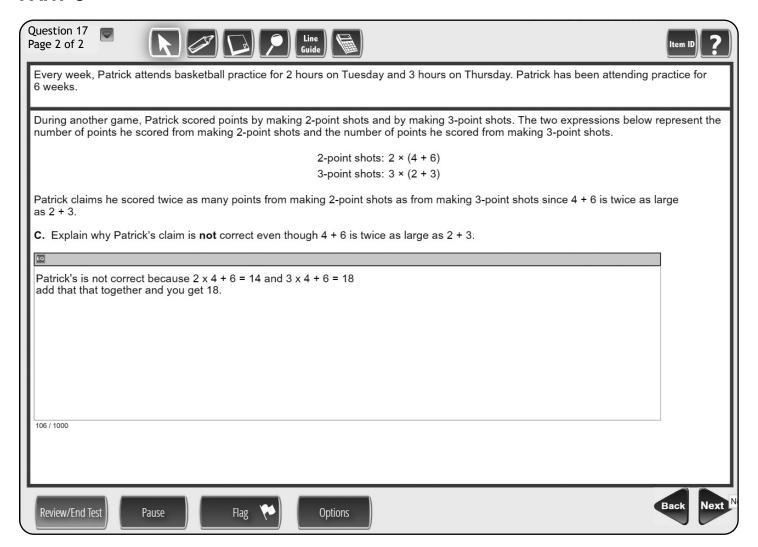
#### **PARTS A and B**



Part A. The student provided an incorrect answer in the form of an equation  $(2 \times 3 \div 6 = 36)$ . The left side of the equation provided is incorrect: the student used a multiplication sign between 2 and 3 rather than an addition sign, did not put grouping symbols around the 2 and 3, and then divided the total by 6 rather than multiplying the total by 6. The right side of the equation (36) does not match the expression on the left side, which has a value of 1. [0 points]

Part B. The student provided an incorrect answer (14) with incorrect support. The student rewrote the given expression and then incorrectly reordered the expression  $(4 + 3 \times 1 + 2 \times 2 + 3)$ , resulting in an incorrect answer of 14. [0 points]

#### **PART C**



Part C. The student provided an incorrect explanation (Patrick's is not correct because  $2 \times 4 + 6 = 14$  and  $3 \times 4 + 6 = 18$  add that that together and you get 18). The student has incorrectly calculated the total points for 2-point shots by not distributing the 2 to both the 4 and the 6. The expression for the 3-point shots is also incorrectly rewritten (using 4 + 6 rather than 2 + 3) and incorrectly calculated (not distributing the 3 to both numbers). The student did not make any references to the multipliers and did not make a comparison between the two point totals. [0 points]

## MATHEMATICS—SUMMARY DATA

# **Multiple-Choice**

Sample Number	Alignment	Answer Key	Depth of Knowledge	<i>p</i> -value A	<i>p</i> -value B	<i>p</i> -value C	<i>p</i> -value D
1	A-T.2.1.3	А	1	59%	8%	27%	6%
2	A-T.1.1.3	D	1	15%	9%	17%	59%
3	A-T.1.1.4 A-T.1.1.3	В	1	16%	48%	32%	4%
4	A-T.2.1	D	2	13%	11%	8%	68%
5	A-T.2.1.2 A-T.2.1.1	А	1	62%	10%	8%	20%
6	A-F.1.1.1	В	2	12%	51%	23%	14%
7	A-F.2.1	D	2	17%	20%	26%	37%
8	A-F.2.1.1	С	1	29%	18%	43%	10%
9	A-F.2.1.3	В	2	15%	48%	14%	23%
10	A-F.2.1.4	D	2	27%	15%	10%	48%
11	C-G.1	С	2	20%	18%	48%	14%
12	C-G.1.1.1	С	1	17%	13%	53%	17%
13	C-G.1.1.2	А	1	63%	19%	12%	6%
14	C-G.2.1.1	D	1	10%	10%	15%	65%
15	D-M.1.1.1	D	2	15%	16%	31%	38%
16	D-M.3.1.2	В	2	31%	40%	18%	11%

# **Open-Ended**

Sample Number	Alignment	Points	Depth of Knowledge	Mean Score
17	B-O.1.1.1 B-O.1.1.2	4	2	1.43

# **PSSA Grade 5 Mathematics Item and Scoring Sampler**

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